## Malbank School Mathematics Curriculum

Intent: In Malbank's Mathematics Department we aim to develop confident and enthusiastic mathematicians who understand the relevance, value and beauty of mathematics and its place in the world. We will give students opportunities to look more deeply into mathematical concepts and where they can be used, so that they can see the links between the different aspects of the course to help them gain a greater understanding of the subject.

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| Knowledge and progression of topics over the 5 years are broken down into the categories of: <br> 1. Number <br> 2. Algebra <br> 3. Ratio \& Proportion <br> 4. Geometry and Measure <br> 5. Statistics <br> 6. Probability <br> The progression routes for these are on the following pages. | Throughout the Maths curriculum and years we look to develop learners who demonstrate: <br> - Resilience <br> - Good communicators <br> - Good organisers, both written, verbal and mathematically <br> - Initiative <br> - Self-motivated <br> - Supportive <br> - Reflective <br> - Inquisitive <br> - Positive learners | The skills we nurture and develop throughout the Maths curriculum are: <br> - To write mathematically and logically <br> - Understand and use mathematical terminology and notation <br> - Interpret problems <br> - Apply mathematical knowledge to different contexts and understand how Maths can be used in the wider world <br> - Link different topics together <br> - Realise there can be multiple routes to solutions |


| 1. Number |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 7 | 8 | 9 | 10 | 11 |
| order positive and negative integers | order positive and negative decimals and fractions use the symbols $=, \neq,\langle\rangle,, \leq$, $\geq$ | Revisit through all situations e.g. when collecting like terms and simplifying expressions | Revisit through all situations e.g. when collecting like terms and simplifying expressions | Revisit through all situations e.g. when collecting like terms and simplifying expressions |
| Apply the four operations, including formal written methods, to integers both positive and negative | apply the four operations, including decimals and fractions |  |  |  |
| Understand and use place value - multiplying and dividing by $10,100,1000$ | understand and use place value multiplying and dividing by powers of 10 | Write large and small numbers in standard form | Calculate with and interpret standard form |  |
| Recognise and use relationships between operations. Use conventional notation for priority of operations | recognise and use relationships between operations, including inverse operations Understand and use BIDMAS |  |  |  |
| Understand factors, multiples and use to find HCFs \& LCMs | Write all numbers as a product of their prime factors |  |  |  |
|  | apply systematic listing strategies |  | Use of the product rule for counting for counting |  |
| use positive integer powers and square and cube roots | use positive integer powers and associated real roots (square, cube and higher), recognise powers of 2, 3, 4, 5 |  | estimate powers and roots of any given positive number |  |
| calculate with roots, and with integer indices |  | Know and understand negative indices | calculate with fractional indices |  |
| calculate exactly with fractions | calculate exactly with multiples of pi |  | calculate exactly with surds simplify surd expressions involving squares and rationalise denominators |  |
| work interchangeably with terminating decimals and their corresponding fractions |  | change recurring decimals into their corresponding fractions and vice versa |  |  |
| interpret fractions and percentages as operators | identify and work with fractions in ratio problems | including interpreting percentage problems using a multiplier. |  |  |
| use standard units of mass, length, time, money and other measures using decimal quantities where appropriate. Know and use metric conversion factors for length, | use standard units of mass, length, time, money and other measures (including standard compound measures) using decimal quantities where appropriate | know and use metric conversion factors for length, area, volume and capacity. |  |  |
| round numbers and measures to an appropriate degree of accuracy | estimate answers <br> check calculations using approximation and estimation | use inequality notation to specify simple error intervals due to truncation or rounding | apply and interpret limits of accuracy including upper and lower bounds |  |


| 2. Algebra (Part 1) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Year 7 | Year 8 | Year 9 | Year 10 | Year 11 |
| A1 | Use and interpret algebraic notation, including coefficients written as fractions rather than as decimals brackets |  |  |  |  |
| A2 | Substitute into basic expressions | Substitution into more complex expressions and formulae (including scientific) |  |  |  |
| A3 | Substitution into more complex expressions and formulae (including scientific) | Recap vocabulary from year 7, extend to looking at identities, formulae and inequalities |  |  |  |
| A4 | Collect like terms Expand single brackets Factorise single brackets | Expand and simplify expressions with multiple brackets | Simplify expressions involving indices <br> Expanding 2 binomials <br> Factorising quadratics | Expanding two or more binomials Factorising quadratics of the form $a x^{\wedge} 2+b x+c$, including difference of two squares. <br> Expanding and simplifying including laws of surds. | Simplify and manipulate algebraic fractions |
| A5 |  | Understand and use standard formulae | Rearrange formulae to change the subject | Rearrange formulae to change the subject where the unknown appears more than once |  |
| A6 |  | Know the difference between identities and equations |  | Produce mathematical arguments and algebraic proofs |  |
| A7 | Use function machines to find inputs and outputs |  |  |  | Function notation including inverse and composite functions |
| A8 | Read and plot coordinates in all 4 quadrants |  |  |  |  |
| A9 |  | Plot linear graphs from the coordinates | Recognise gradients and intercepts of linear graphs. <br> Recognise parallel graphs | Find the equation of a line given 2 points. Calculate equations of perpendicular lines |  |
| A10 |  |  | Identify and interpret gradients and intercepts of linear functions graphically and algebraically, using real life examples |  |  |
| A11 |  | Factorise basic quadratics | Solve quadratic equations by factorising Solve quadratic equations using the formula Find approximate solutions from graphs | Solve quadratics by completing the square |  |
| A12 |  |  | Plot quadratic equiations, identifying roots, intercepts and turning points of quadratic equations | Deduce turning points by completing the square |  |


| 2. Algebra (Part 2) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Year 7 | Year 8 | Year 9 | Year 10 | Year 11 |
| A13 |  |  | Recognise, sketch and interpret graphs of linear and quadratic functions |  | Plotting and sketching simple cubic, and reciprocal functions <br> Plotting and sketching exponential functions and trigonometric functions |
| A14 |  |  |  |  | Sketch translations and reflections of a given function |
| A15 |  | Plot real life graphs, including speed distance time | Plot real life graphs, including speed distance time | Plot real life graphs including reciprocals and exponentials |  |
| A16 |  |  |  | Calculate and estimate gradients of graphs are areas under graphs and interpret results |  |
| A17 |  |  |  |  | Recognise and use the equation of a circle with centre at the origin Find the equation of a tangent to a circle at a point |
| A18 | Solve linear equations in one unknown algebraically | Solve linear equations with unknowns on both sides | Find approximate solutions to linear solutions using a graph |  |  |
| A19 |  |  | Solve two simultaneous equations in two variable (linear/linear) algebraically Find approximate solutions to simultaneous equations using a graph | Solve linear/quadratic simultaneous equations algebraically and graphically |  |
| A20 |  |  |  |  | Find approximate solutions to equations numerically using iteration |
| A21 | Translate simple situations into algebraic expressions | Translate simple algebraic situations into expressions and formulae and substitute to solve | Derive an equation or two simultaneous equations and solve the equations and interpret the solutions |  |  |
| A22 |  | Find integer solutions to inequalities | Solve linear inequalities in one variable Represent the solution set on a number line | Solve linear inequalities in one or two variables and quadratic inequalities in one variable <br> Represent the solution set on using set notation and regions on a graph |  |
| A23 | Generate terms of a sequence from term to term rules, including patterns and diagrams | Generate terms of a sequence using a position to term rule |  |  |  |
| A24 | Recognise and use sequences of triangular, square and cube numbers | Recognise and use Fibonacci-type sequences and quadratic sequences | Recognise and use simple geometric progressions | Recognise and use other sequences including using surds |  |
| A25 | Write nth term rules for linear sequences |  | Write nth term rules for quadratic sequences |  |  |


| 3. Ratio \& Proportion |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Year 7 | Year 8 | Year 9 | Year 10 | Year 11 |
| R1 - change freely between related standard units (eg time, length, area, volume/capacity, mass) | R1 - change freely between related standard units (eg speed, rates of pay, prices) in numerical contexts | R1-compound units (eg density, pressure) | R1-in numerical and algebraic contexts | R5 -apply ratio to real contexts and problems (such as those involving conversion, comparison, scaling, mixing, concentrations) |
| R2-Scales | R3 - express one quantity as a fraction of another, where the fraction is less than 1 or greater than 1 | R2-scale factors | R2 - scale factors, scale diagrams and maps | R9 -solve problems involving percentage change, including percentage increase/decrease and original value problems, and simple interest including in financial mathematics |
| R4- use ratio notation, including reduction to simplest form | R5 -apply ratio to real contexts and problems (such as those involving conversion, comparison, scaling, mixing, concentrations) | R5 -apply ratio to real contexts and problems <br> (such as those involving conversion, comparison, scaling, mixing, concentrations) | R5 -apply ratio to real contexts and problems (such as those involving conversion, comparison, scaling, mixing, concentrations) | solve problems including graphical and algebraic representations |
| R5 -divide a given quantity into two parts in a <br> given part : part or part : whole ratio express <br> the division of a quantity into two parts as a <br> ratio apply ratio to real contexts and <br> problems (such as those involving conversion, <br> comparison, scaling, mixing, concentrations) | R8-relate ratios to fractions | R6- express a multiplicative relationship between two quantities as a ratio or a fraction | R9 -solve problems involving percentage change, including percentage increase/decrease and original value problems, and simple interest including in financial mathematics | R13 - construct and interpret equations that describe direct and inverse proportion |
| R7- understand and use proportion as equality of ratios | R9 - compare two quantities using percentages solve problems involving percentage change, including percentage increase/decrease and original value problems, and simple interest including in financial mathematics | R8 - relate ratios to linear functions | R10 - solve problems involving direct and inverse proportion | R14 - interpret the gradient of a straight-line graph as a rate of change recognise and interpret graphs that illustrate direct and inverse proportion |
| R9 - define percentage as 'number of parts per hundred' interpret percentages and percentage changes as a fraction or a decimal, and interpret these multiplicatively express one quantity as a percentage of another work with percentages greater than $100 \%$ Solve problems |  | R9 -solve problems involving percentage change, including percentage increase/decrease and original value problems, and simple interest including in financial mathematics | R11 - use compound units such as density and pressure | R15 - interpret the gradient at a point on a curve as the instantaneous rate of change apply the concepts of average and instantaneous rate of change (gradients of chords and tangents) in numerical, algebraic and graphical contexts |
|  |  | R11 - use compound units such as speed, rates of pay, unit pricing | R12 - make links to similarity (including trigonometric ratios) | R16 - set up, solve and interpret the answers in growth and decay problems, including compound interest and work with general iterative processes |
|  |  | R12 - compare lengths, areas and volumes using ratio notation scale factors | R13 - understand that $X$ is inversely proportional to Y is equivalent to $X$ is proportional to interpret equations that describe direct and inverse proportion |  |
|  |  |  | R16 - set up, solve and interpret the answers in compound interest |  |


| 4. Geometry \& Measures |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Year 7 | Year 8 | Year 9 | Year 10 | Year 11 |
| 2D \& 3D Shape Properties | Bisectors | Loci |  |  |
| Angles on a line/point/vertically opposite/triangle | Angles on parallel lines \& polygons | Bearings \& Scale Drawings |  |  |
| Lines of symmetry <br> Reflection in a mirror lineRotation from a given point <br> Translations using words Enlargement with a scale factor Rotational symmetry | Reflections with an equation of a line Rotation about a co-ordinate point <br> Translations with vectors Enlargement from a point | Enlargement with a fractional scale factor Column vectors (Addition, subtraction \& multiplication) | Enlargement with a negative scale factor Vector proofs | Describe transformation invariants. |
| Perimeter and area rectangles, triangles, parallelograms, trapeziums, compound Properties of circles radius/diameter/circumference S.A. cuboids/triangular prisms | Circumference and area of circles/semicircles <br> S.A. cylinders <br> Volume prisms | Area and perimeter - Sectors <br> S.A. sphere/cone <br> Volume - cone/sphere/pyramid <br> Circle properties - <br> tangent/arc/sector/segment | Area using trig 1/2absinC Volume frustums | Circle theorems |
|  |  | Congruence/similarity |  | Similarity - area \& volume |
|  | Pythag | Trig (right-angled) | Trig - 3D/non-right angled | Trig exact values |
|  | Convert metric units | Converting time | Converting measures of area \& volume |  |
|  |  |  | Solve geometric problems on coordinate axes |  |
|  | Plans \& elevations |  |  |  |



| 6. Probability |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Year 7 | Year 8 | Year 9 | Year 10 | Year 11 |
| P1 | Know the difference between theoretical and experimental probability. Conduct probability experiments and record outcomes appropriately. | Analyse the frequency of outcomes using frequency trees and two way tables |  |  |  |
| P2 | Understand concepts of randomness, fairness and equally likely events. | Calculate expected outcomes of multiple future experiments |  |  |  |
| $\begin{array}{\|c\|} \hline \mathrm{P} 3 / \mathrm{P} 4 / \\ \text { P5 } \end{array}$ | Introduce the probability scale and know the appropriate language for probability. Understand that 1 is the largest probability of an event occuring | Apply the property that the probabilities of an exhaustive set of outcomes sum to 1 - use this to find probabilities of events not happening | Compare relative frequency to theoretical probability <br> Know that the more you do an experiment; the more accurate the results will become |  |  |
| P6/P7 |  | List outcomes systematically | Construct theoretical possibility spaces for single and combined experiments with equally likely outcomes and use these to calculate theoretical probabilities |  |  |
| P8/P9 |  | Use tree diagrams to show the probability of combined independent events | Use tree diagrams to show the probability of dependent events | Calculate probabilities of successive dependent events <br> Calculate and interpret conditional probabilities through representation using expected frequencies Know when to add and when to multiply two or more probabilities | Calculate probabilities using Venn diagrams and set notation. |

